

Answer Set Programming modulo Acyclicity

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LPNMR'15, Lexington, Kentucky, USA, September 30, 2015

Translation-Based ASP

ASP can be implemented by translating ground programs into:

- Boolean Satisfiability (SAT)
 [J., ECAI 2004; J. and Niemelä, MG-65 2010]
- Integer Difference Logic (IDL)
 [Niemelä, AMAI 2008; J. et al., LPNMR 2009]
- Integer Programming (IP) [Liu et al., KR 2012]
- Bit-Vector Logic (BV) [Nguyen et al., INAP 2011; Extended in 2013]



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- SAT modulo Acyclicity (ACYC-SAT) [G. et al., ECAI 2014]



Extensions to ASP

There are existing SMT-style extensions of ASP:

- Constraint programming [G. et al., ICLP 2009]
- Difference logic [J. et al., GTTV 2011]
- Linear programming [Liu et al., INAP 2013]
- General SMT [Lee & Meng, IJCAI 2013]



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 - as an extension to ASP and
 - as a target formalism for translations of ASP.



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 - as an extension to ASP and
 - as a target formalism for translations of ASP.
- ► Functionality available in CLASP version 3.2.0 onward.



Standard Logic Programs

Logic programs consist of rules of the following forms:

$$a \leftarrow b_1, \dots, b_n, \text{ not } c_1, \dots, \text{ not } c_m.$$

$$\{a\} \leftarrow b_1, \dots, b_n, \text{ not } c_1, \dots, \text{ not } c_m.$$

$$a \leftarrow k \le [b_1 = w_1, \dots, b_n = w_n,$$

$$\text{ not } c_1 = w_{n+1}, \dots, \text{ not } c_m = w_{n+m}].$$

► A model is supported [Apt et al., 1988] iff $M = T_{P^M}(M)$ and stable [Gelfond and Lifschitz, ICLP 1988] iff $M = LM(P^M)$.



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► A model is supported [Apt et al., 1988] iff M = T_{PM}(M) and stable [Gelfond and Lifschitz, ICLP 1988] iff M = LM(P^M).
Example

$$a \leftarrow b$$
. $a \leftarrow c$. $b \leftarrow a$. $c \leftarrow not d$. $d \leftarrow not c$.

 \implies $M_1 = \{a, b, c\}$ and $M_2 = \{a, b, d\}$ are both supported, and M_1 is also stable.



Acyclicity Extension

An acyclicity extension is a pair $\langle V, e \rangle$ where

- 1. V is a set of vertices and
- e : At(P) → V × V is a partial injection that maps atoms of a logic program P to edges.



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- 2. $e: At(P) \rightarrow V \times V$ is a partial injection that maps atoms of a logic program *P* to edges.

An interpretation $M \subseteq At(P)$ is a stable/supported model of P subject to an acyclicity extension $\langle V, e \rangle$, iff

- 1. *M* is a stable/supported model of *P* and
- 2. the graph $\langle V, e(M) \rangle$ is acyclic, where $e(M) = \{ \langle v, u \rangle \in V \times V \mid a \in M, e(a) = \langle v, u \rangle \}.$









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1 { hc(X,Y) : edge(X,Y) } 1 :- node(X). 1 { hc(X,Y) : edge(X,Y) } 1 :- node(Y). _edge(X,Y) :- hc(X,Y), X > 1, Y > 1.

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Example: Acyclicity Constraints

Let us consider a standard logic program

$$a \leftarrow b$$
. $a \leftarrow c$. $b \leftarrow a$. $c \leftarrow \text{not } d$. $d \leftarrow \text{not } c$.
_edge $(a, b) \leftarrow a$, not c. _edge $(b, a) \leftarrow b$.

and extend it by $\langle V, e \rangle$ where $V = \{a, b\}$ and e is the mapping

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 $\implies M_1 = \{a, b, c, _edge(b, a)\} \text{ is a stable and supported model};$ $M_2 = \{a, b, d, _edge(a, b), _edge(b, a)\} \text{ is neither.}$



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Translation from ASP to ACYC-ASP

- We define a translation Tr_{ACYC}(P) that extends P by an acyclicity extension and a set of rules.
- The stable models of P coincide with the stable/supported models of Tr_{ACYC}(P) modulo acyclicity.
- Well-support of answer sets can be addressed by performing on Tr_{ACYC}(P) one or both of
 - unfounded set checking or
 - acyclicity checking.



Tool Support



These tools are published under:

http://research.ics.aalto.fi/software/asp/lp2acyc/ http://potassco.sourceforge.net/projects/potassco/



Experiments: Decision Problems

Mode	Cycle #60		<i>Laby</i> #20		<i>Soko</i> #30		Route #23	
UFS	36.0	0	255.3	4	182.6	2	5.8	0
ACYC	373.6	37	261.0	6	350.7	10	134.5	4
BCYC	266.3	26	286.7	7	256.2	7	111.5	2
ACYC/UFS	209.4	18	279.2	4	174.6	3	11.4	0
BCYC/UFS	209.2	19	314.3	6	179.7	4	10.0	0
ACYC+	118.0	7	366.7	7	336.7	10	137.2	4
BCYC+	85.3	5	279.6	5	230.4	5	138.6	4
ACYC+/UFS	115.9	8	311.8	5	176.6	4	15.4	0
BCYC+/UFS	91.9	6	212.7	4	170.2	3	12.3	0

- ACYC: Acyclicity checking UFS: Unfounded set checking
- BCYC: ACYC with backward propagation
- - +: Extended translation



Experiments: Optimization Problems

Mode	Bayes #30		Markov #	‡ 21	Sched #18		
UFS	116.8	0	100.7	0	281.2	7	
ACYC	66.3	0	120.3	1	320.9	8	
BCYC	84.6	0	54.1	0	324.2	7	
ACYC/UFS	103.1	1	170.2	3	348.2	9	
BCYC/UFS	104.3	1	72.5	0	340.3	9	
ACYC+	106.2	1	61.5	0	340.9	9	
BCYC+	102.2	2	39.9	0	341.1	9	
ACYC+/UFS	110.3	1	171.4	3	367.5	9	
BCYC+/UFS	122.5	2	111.5	1	360.6	9	

- BCYC: ACYC with backward propagation
- ACYC: Acyclicity checking UFS: Unfounded set checking
 - +: Extended translation



Conclusion

- We propose ASP modulo Acyclicity
 - to help in application areas involving DAGs, trees, etc., and
 - to embed ASP into itself.
- Well-support of answer sets can be addressed by acyclicity checking
- Implementation is built into the tools lp2acyc and clasp

